

Winter Term 2026/27

Selected Topics in Deep Learning for Audio, Speech, and Music Processing

Lecture

Nonnegative Music Audio Decomposition

Stefan Balke, Andreas Brendel, Ben Maman, Meinard Müller

Source Separation

- Decomposition of audio stream into different sound sources
- Central task in digital signal processing
- “Cocktail party effect”

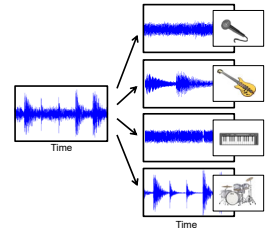


Source Separation

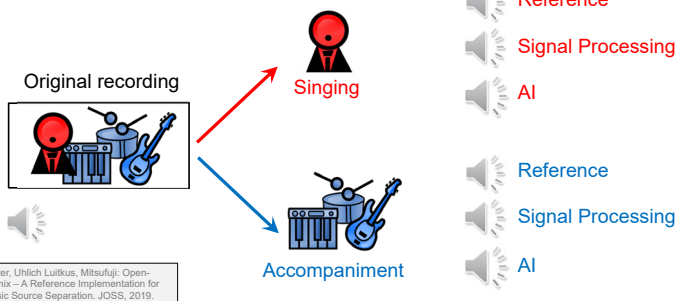
- Decomposition of audio stream into different sound sources
- Central task in digital signal processing
- “Cocktail party effect”
- Several input signals
- Sources are assumed to be statistically independent

Source Separation

- Main melody, accompaniment, drum track
- Instrumental voices
- Individual note events
- Only mono or stereo
- Sources are often highly dependent

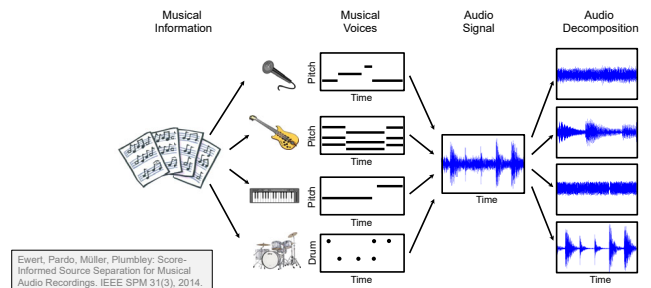


Source Separation Singing Voice



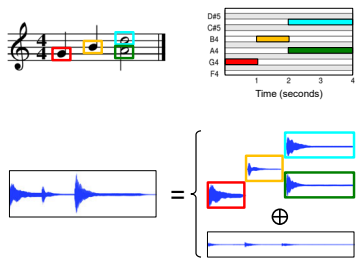
Score-Informed Source Separation

Exploit musical score to support decomposition process



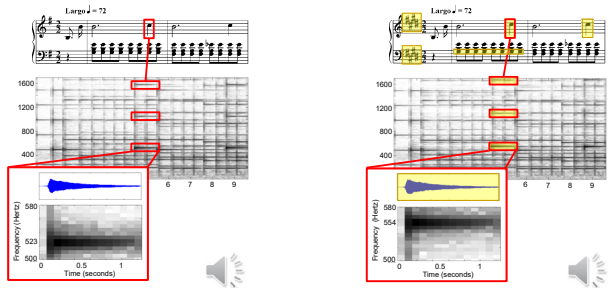
Score-Informed Audio Decomposition

Driedger, Grohgan, Prätzlich, Ewert, Müller: Score-Informed Audio Decomposition and Applications. Proc. ACM Multimedia: 541–544, 2013



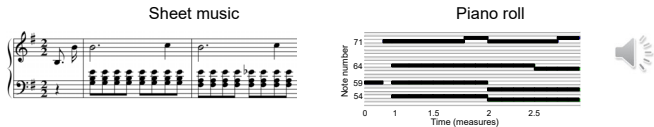
Score-Informed Audio Decomposition

Driedger, Grohgan, Prätzlich, Ewert, Müller: Score-Informed Audio Decomposition and Applications. Proc. ACM Multimedia: 541–544, 2013



Score-Informed Audio Decomposition

Ewert, Pardo, Müller, Plumbley: Score-Informed Source Separation for Musical Audio Recordings. IEEE Signal Proc. Mag. 31(3): 116–124, 2014



Score-Informed Audio Decomposition

Ewert, Pardo, Müller, Plumbley: Score-Informed Source Separation for Musical Audio Recordings. IEEE Signal Proc. Mag. 31(3): 116–124, 2014



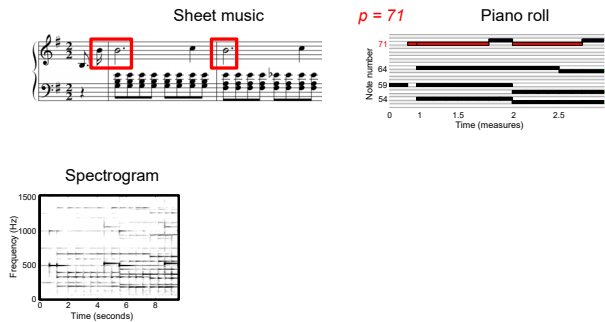
Score-Informed Audio Decomposition

Ewert, Pardo, Müller, Plumbley: Score-Informed Source Separation for Musical Audio Recordings. IEEE Signal Proc. Mag. 31(3): 116–124, 2014



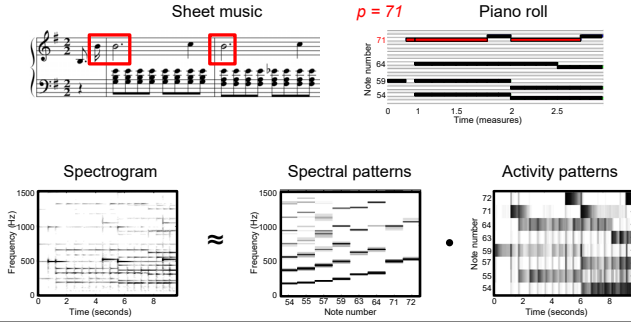
Score-Informed Audio Decomposition

Ewert, Pardo, Müller, Plumbley: Score-Informed Source Separation for Musical Audio Recordings. IEEE Signal Proc. Mag. 31(3): 116–124, 2014



Score-Informed Audio Decomposition

Ewert, Pardo, Müller, Plumbley: Score-Informed Source Separation for Musical Audio Recordings. IEEE Signal Proc. Mag. 31(3): 116–124, 2014



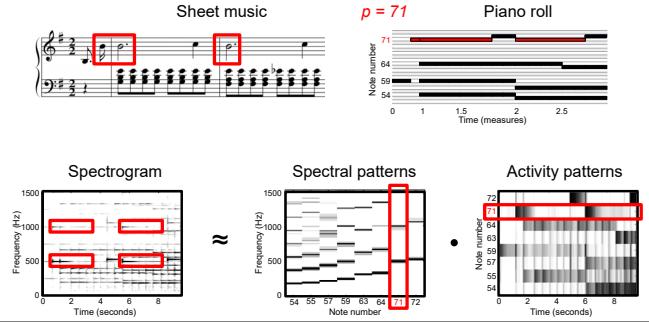
© AudioLabs, 2026
Meinard Müller

Nonnegative Music Audio Decomposition
13

AUDIO
LABS

Score-Informed Audio Decomposition

Ewert, Pardo, Müller, Plumbley: Score-Informed Source Separation for Musical Audio Recordings. IEEE Signal Proc. Mag. 31(3): 116–124, 2014



© AudioLabs, 2026
Meinard Müller

Nonnegative Music Audio Decomposition
14

AUDIO
LABS

Nonnegative Matrix Factorization (NMF)

$$\begin{array}{c} N \\ K \quad V \\ \geq 0 \end{array} \approx \begin{array}{c} R \\ K \quad W \\ \geq 0 \end{array} \bullet \begin{array}{c} N \\ H \\ \geq 0 \end{array} \begin{array}{c} R \\ \geq 0 \end{array}$$

$V \in \mathbb{R}_{\geq 0}^{K \times N}$ $W \in \mathbb{R}_{\geq 0}^{K \times R}$ $H \in \mathbb{R}_{\geq 0}^{R \times N}$

© AudioLabs, 2026
Meinard Müller

Nonnegative Music Audio Decomposition
15

AUDIO
LABS

Nonnegative Matrix Factorization (NMF)

$$\begin{array}{c} N \\ K \quad V \\ \geq 0 \end{array} \approx \begin{array}{c} R \\ K \quad W \\ \geq 0 \end{array} \bullet \begin{array}{c} N \\ H \\ \geq 0 \end{array} \begin{array}{c} R \\ \geq 0 \end{array}$$

Magnitude Spectrogram **Templates** **Activations**

Templates: Pitch + Timbre

“How does it sound”

Activations: Onset time + Duration “When does it sound”

© AudioLabs, 2026
Meinard Müller

Nonnegative Music Audio Decomposition
16

AUDIO
LABS

Nonnegative Matrix Factorization (NMF)

$$\begin{array}{c} N \\ K \quad V \\ \geq 0 \end{array} \approx \begin{array}{c} R \\ K \quad W \\ \geq 0 \end{array} \bullet \begin{array}{c} N \\ H \\ \geq 0 \end{array} \begin{array}{c} R \\ \geq 0 \end{array}$$

$V \in \mathbb{R}_{\geq 0}^{K \times N}$ $W \in \mathbb{R}_{\geq 0}^{K \times R}$ $H \in \mathbb{R}_{\geq 0}^{R \times N}$

Dimensionality reduction

- K, N typically much larger than R (maximal rank)
- Example: $N = 1000$, $K = 500$, $R = 20$
 $K \times N = 500,000$, $K \times R = 10,000$, $R \times N = 20,000$

© AudioLabs, 2026
Meinard Müller

Nonnegative Music Audio Decomposition
17

AUDIO
LABS

Nonnegative Matrix Factorization (NMF)

$$\begin{array}{c} N \\ K \quad V \\ \geq 0 \end{array} \approx \begin{array}{c} R \\ K \quad W \\ \geq 0 \end{array} \bullet \begin{array}{c} N \\ H \\ \geq 0 \end{array} \begin{array}{c} R \\ \geq 0 \end{array}$$

$V \in \mathbb{R}_{\geq 0}^{K \times N}$ $W \in \mathbb{R}_{\geq 0}^{K \times R}$ $H \in \mathbb{R}_{\geq 0}^{R \times N}$

Nonnegativity:

- Prevents mutual cancellation of template vectors
- Encourages semantically meaningful decomposition

© AudioLabs, 2026
Meinard Müller

Nonnegative Music Audio Decomposition
18

AUDIO
LABS

NMF Optimization

Optimization problem:

Given $V \in \mathbb{R}_{\geq 0}^{K \times N}$ and rank parameter R minimize

$$\|V - WH\|^2$$

with respect to $W \in \mathbb{R}_{\geq 0}^{K \times R}$ and $H \in \mathbb{R}_{\geq 0}^{R \times N}$.

Optimization not easy:

- Nonnegativity constraints
- Nonconvexity when jointly optimizing W and H

Strategy: Iteratively optimize W and H via gradient descent

NMF Optimization

Computation of gradient with respect to H (fixed W)

$$D := RN$$

$$\phi^W : \mathbb{R}^D \rightarrow \mathbb{R}$$

$$\phi^W(H) := \|V - WH\|^2$$

Variables

$$H \in \mathbb{R}^{R \times N}$$

$$H_{\rho v}$$

$$\rho \in [1 : R]$$

$$v \in [1 : N]$$

NMF Optimization

Computation of gradient with respect to H (fixed W)

$$D := RN$$

$$\phi^W : \mathbb{R}^D \rightarrow \mathbb{R}$$

$$\phi^W(H) := \|V - WH\|^2$$

$$\frac{\partial \phi^W}{\partial H_{\rho v}} = \frac{\partial \left(\sum_{k=1}^K \sum_{n=1}^N (V_{kn} - \sum_{r=1}^R W_{kr} H_{rn})^2 \right)}{\partial H_{\rho v}}$$

Variables

$$H \in \mathbb{R}^{R \times N}$$

$$H_{\rho v}$$

$$\rho \in [1 : R]$$

$$v \in [1 : N]$$

NMF Optimization

Computation of gradient with respect to H (fixed W)

$$D := RN$$

$$\phi^W : \mathbb{R}^D \rightarrow \mathbb{R}$$

$$\phi^W(H) := \|V - WH\|^2$$

$$\frac{\partial \phi^W}{\partial H_{\rho v}} = \frac{\partial \left(\sum_{k=1}^K \sum_{n=1}^N (V_{kn} - \sum_{r=1}^R W_{kr} H_{rn})^2 \right)}{\partial H_{\rho v}} = \frac{\partial \left(\sum_{k=1}^K (V_{kv} - \sum_{r=1}^R W_{kr} H_{rv})^2 \right)}{\partial H_{\rho v}}$$

Variables

$$H \in \mathbb{R}^{R \times N}$$

$$H_{\rho v}$$

$$\rho \in [1 : R]$$

$$v \in [1 : N]$$

Summand that does not depend on $H_{\rho v}$ must be zero

NMF Optimization

Computation of gradient with respect to H (fixed W)

$$D := RN$$

$$\phi^W : \mathbb{R}^D \rightarrow \mathbb{R}$$

$$\phi^W(H) := \|V - WH\|^2$$

$$\frac{\partial \phi^W}{\partial H_{\rho v}} = \frac{\partial \left(\sum_{k=1}^K \sum_{n=1}^N (V_{kn} - \sum_{r=1}^R W_{kr} H_{rn})^2 \right)}{\partial H_{\rho v}} = \frac{\partial \left(\sum_{k=1}^K (V_{kv} - \sum_{r=1}^R W_{kr} H_{rv})^2 \right)}{\partial H_{\rho v}}$$

Apply chain rule from calculus

Variables

$$H \in \mathbb{R}^{R \times N}$$

$$H_{\rho v}$$

$$\rho \in [1 : R]$$

$$v \in [1 : N]$$

NMF Optimization

Computation of gradient with respect to H (fixed W)

$$D := RN$$

$$\phi^W : \mathbb{R}^D \rightarrow \mathbb{R}$$

$$\phi^W(H) := \|V - WH\|^2$$

$$\frac{\partial \phi^W}{\partial H_{\rho v}} = \frac{\partial \left(\sum_{k=1}^K \sum_{n=1}^N (V_{kn} - \sum_{r=1}^R W_{kr} H_{rn})^2 \right)}{\partial H_{\rho v}} = \frac{\partial \left(\sum_{k=1}^K (V_{kv} - \sum_{r=1}^R W_{kr} H_{rv})^2 \right)}{\partial H_{\rho v}}$$

Variables

$$H \in \mathbb{R}^{R \times N}$$

$$H_{\rho v}$$

$$\rho \in [1 : R]$$

$$v \in [1 : N]$$

Rearrange summands

$$= \sum_{k=1}^K 2 \left(V_{kv} - \sum_{r=1}^R W_{kr} H_{rv} \right) \cdot (-W_{k\rho}) = 2 \left(\sum_{r=1}^R \sum_{k=1}^K W_{kr} W_{kr} H_{rv} - \sum_{k=1}^K W_{k\rho} V_{kv} \right)$$

NMF Optimization

Computation of gradient with respect to H (fixed W)

$$\begin{aligned}
 D &:= RN \\
 \phi^W : \mathbb{R}^D &\rightarrow \mathbb{R} \\
 \phi^W(H) &:= \|V - WH\|^2 \\
 \frac{\partial \phi^W}{\partial H_{\rho\nu}} &= \frac{\partial \left(\sum_{k=1}^K \sum_{n=1}^N (V_{kn} - \sum_{r=1}^R W_{kr} H_{rn})^2 \right)}{\partial H_{\rho\nu}} \\
 &= \frac{\partial \left(\sum_{k=1}^K (V_{k\nu} - \sum_{r=1}^R W_{kr} H_{rv})^2 \right)}{\partial H_{\rho\nu}} \\
 &= \sum_{k=1}^K 2 \left(V_{k\nu} - \sum_{r=1}^R W_{kr} H_{rv} \right) \cdot (-W_{k\rho}) \\
 &= 2 \left(\sum_{r=1}^R \sum_{k=1}^K W_{k\rho} W_{kr} H_{rv} - \sum_{k=1}^K W_{k\rho} V_{k\nu} \right) \\
 &= 2 \left(\sum_{r=1}^R \left(\sum_{k=1}^K W_{\rho k}^\top W_{kr} \right) H_{rv} - \sum_{k=1}^K W_{\rho k}^\top V_{k\nu} \right)
 \end{aligned}$$

Introduce
transposed $W^\top$

NMF Optimization

Computation of gradient with respect to H (fixed W)

$$\begin{aligned}
 D &:= RN \\
 \phi^W : \mathbb{R}^D &\rightarrow \mathbb{R} \\
 \phi^W(H) &:= \|V - WH\|^2 \\
 \frac{\partial \phi^W}{\partial H_{\rho\nu}} &= \frac{\partial \left(\sum_{k=1}^K \sum_{n=1}^N (V_{kn} - \sum_{r=1}^R W_{kr} H_{rn})^2 \right)}{\partial H_{\rho\nu}} \\
 &= \frac{\partial \left(\sum_{k=1}^K (V_{k\nu} - \sum_{r=1}^R W_{kr} H_{rv})^2 \right)}{\partial H_{\rho\nu}} \\
 &= \sum_{k=1}^K 2 \left(V_{k\nu} - \sum_{r=1}^R W_{kr} H_{rv} \right) \cdot (-W_{k\rho}) \\
 &= 2 \left(\sum_{r=1}^R \sum_{k=1}^K W_{k\rho} W_{kr} H_{rv} - \sum_{k=1}^K W_{k\rho} V_{k\nu} \right) \\
 &= 2 \left(\sum_{r=1}^R \left(\sum_{k=1}^K W_{\rho k}^\top W_{kr} \right) H_{rv} - \sum_{k=1}^K W_{\rho k}^\top V_{k\nu} \right) \\
 &= 2 \left((W^\top WH)_{\rho\nu} - (W^\top V)_{\rho\nu} \right).
 \end{aligned}$$

NMF Optimization

Gradient descent

Initialization $H^{(0)} \in \mathbb{R}^{R \times N}$
Iteration for $\ell = 0, 1, 2, \dots$

$$H_{rn}^{(\ell+1)} = H_{rn}^{(\ell)} - \gamma_{rn}^{(\ell)} \cdot \left((W^\top WH^{(\ell)})_{rn} - (W^\top V)_{rn} \right)$$

with suitable learning rate $\gamma_{rn}^{(\ell)} \geq 0$

NMF Optimization

Gradient descent

Initialization $H^{(0)} \in \mathbb{R}^{R \times N}$
Iteration for $\ell = 0, 1, 2, \dots$

$$H_{rn}^{(\ell+1)} = H_{rn}^{(\ell)} - \gamma_{rn}^{(\ell)} \cdot \left((W^\top WH^{(\ell)})_{rn} - (W^\top V)_{rn} \right)$$

with suitable learning rate $\gamma_{rn}^{(\ell)} \geq 0$

Issues:

- How to do the initialization?
- How to choose the learning rate?
- How to ensure nonnegativity?

NMF Optimization

Gradient descent

Initialization $H^{(0)} \in \mathbb{R}^{R \times N}$
Iteration for $\ell = 0, 1, 2, \dots$

$$\begin{aligned}
 H_{rn}^{(\ell+1)} &= H_{rn}^{(\ell)} - \gamma_{rn}^{(\ell)} \cdot \left((W^\top WH^{(\ell)})_{rn} - (W^\top V)_{rn} \right) \\
 &= H_{rn}^{(\ell)} \cdot \frac{(W^\top V)_{rn}}{(W^\top WH^{(\ell)})_{rn}}
 \end{aligned}$$

Issues:

- How to do the initialization?
- How to choose the learning rate?
- How to ensure nonnegativity?

Choose adaptive
learning rate:

$$\gamma_{rn}^{(\ell)} := \frac{H_{rn}^{(\ell)}}{(W^\top WH^{(\ell)})_{rn}}$$

NMF Optimization

Gradient descent

Initialization $H^{(0)} \in \mathbb{R}^{R \times N}$
Iteration for $\ell = 0, 1, 2, \dots$

$$\begin{aligned}
 H_{rn}^{(\ell+1)} &= H_{rn}^{(\ell)} - \gamma_{rn}^{(\ell)} \cdot \left((W^\top WH^{(\ell)})_{rn} - (W^\top V)_{rn} \right) \\
 &= H_{rn}^{(\ell)} \cdot \frac{(W^\top V)_{rn}}{(W^\top WH^{(\ell)})_{rn}}
 \end{aligned}$$

Issues:

- How to do the initialization?
- How to choose the learning rate?
- How to ensure nonnegativity?

- Update rule become multiplicative
- Nonnegative values stay nonnegative

NMF Optimization

Lee, Seung: Algorithms for Non-Negative Matrix Factorization. Proc. NIPS, 2000

Algorithm: NMF ($V \approx WH$)

Input: Nonnegative matrix V of size $K \times N$
Rank parameter $R \in \mathbb{N}$
Threshold ϵ used as stop criterion

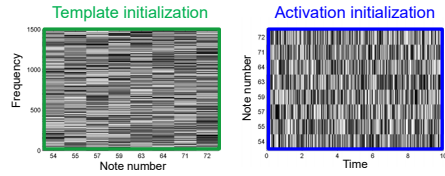
Output: Nonnegative template matrix W of size $K \times R$
Nonnegative activation matrix H of size $R \times N$

Procedure: Define nonnegative matrices $W^{(0)}$ and $H^{(0)}$ by some random or informed initialization. Furthermore set $\ell = 0$. Apply the following update rules (written in matrix notation):

- (1) $H^{(\ell+1)} = H^{(\ell)} \odot ((W^{(\ell)})^T V) \oslash ((W^{(\ell)})^T W^{(\ell)} H^{(\ell)})$
- (2) $W^{(\ell+1)} = W^{(\ell)} \odot (V (H^{(\ell+1)})^T) \oslash (W^{(\ell)} H^{(\ell+1)} (H^{(\ell+1)})^T)$
- (3) Increase ℓ by one.

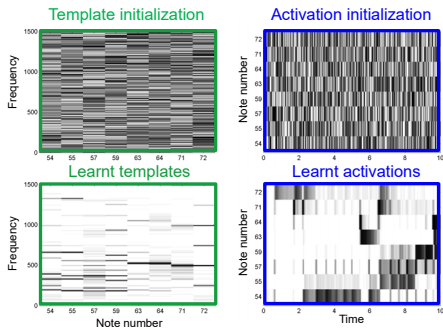
Repeat the steps (1) to (3) until $\|H^{(\ell)} - H^{(\ell-1)}\| \leq \epsilon$ and $\|W^{(\ell)} - W^{(\ell-1)}\| \leq \epsilon$ (or until some other stop criterion is fulfilled). Finally, set $H = H^{(\ell)}$ and $W = W^{(\ell)}$.

NMF-based Spectrogram Decomposition



Random initialization

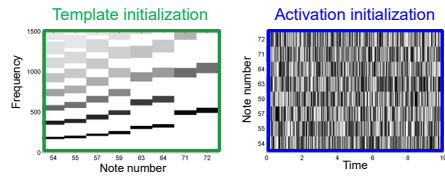
NMF-based Spectrogram Decomposition



Random initialization

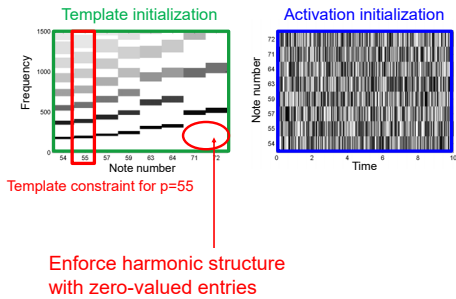
No semantic meaning

Constrained NMF: Templates



Enforce harmonic structure
with zero-valued entries

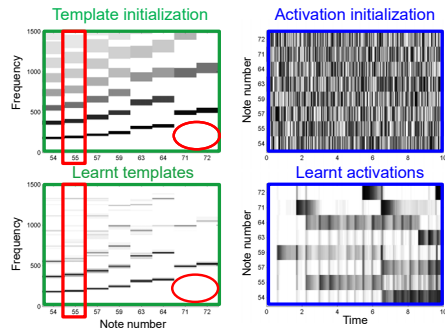
Constrained NMF: Templates



Template constraint for $p=55$

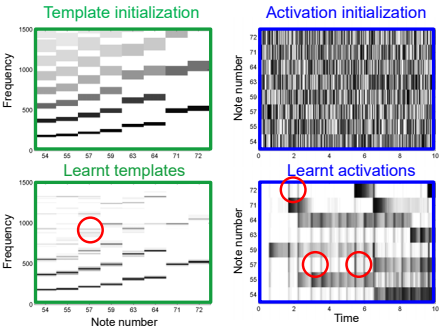
Enforce harmonic structure
with zero-valued entries

Constrained NMF: Templates



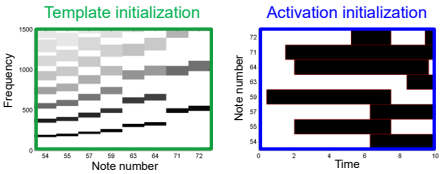
Zero-valued entries
remain zero-valued
entries!

Constrained NMF: Templates

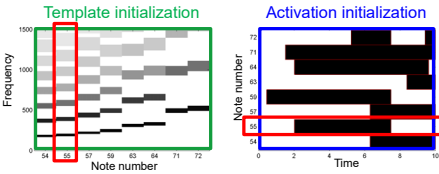


Pitch templates misused to represent onsets

Constrained NMF: Double Constraints



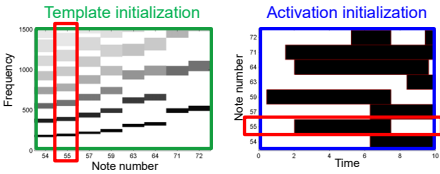
Constrained NMF: Double Constraints



Template constraint for $p=55$

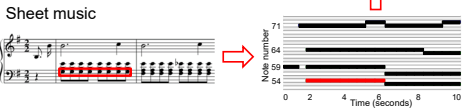
Activation constraints for $p=55$

Constrained NMF: Double Constraints



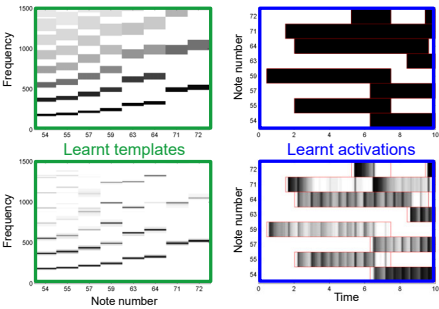
Template constraint for $p=55$

Activation constraints for $p=55$



Such information may come from a synchronized score

Constrained NMF: Double Constraints

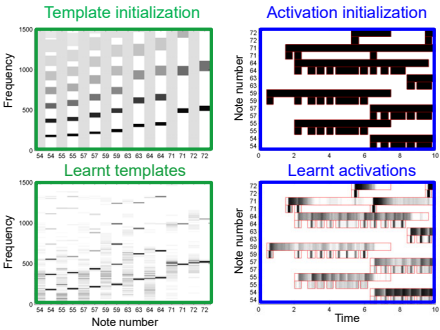


Original

Model

Significant gain, but onsets are missing

Constrained NMF: Onset Templates



Original

Model

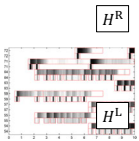
Onsets are sharper

Score-Informed Audio Decompostion

Application: Separating left and right hands for piano



- 1. Split activation matrix

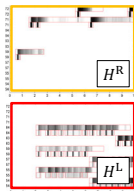


Score-Informed Audio Decompostion

Application: Separating left and right hands for piano



- 1. Split activation matrix

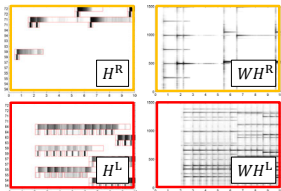


Score-Informed Audio Decompostion

Application: Separating left and right hands for piano



- 1. Split activation matrix
- 2. Model spectrogram for left/right

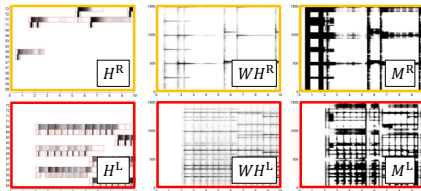


Score-Informed Audio Decompostion

Application: Separating left and right hands for piano



- 1. Split activation matrix
- 2. Model spectrogram for left/right
- 3. Separation masks for left/right

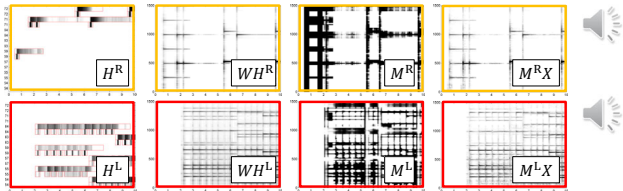


Score-Informed Audio Decompostion

Application: Separating left and right hands for piano



- 1. Split activation matrix
- 2. Model spectrogram for left/right
- 3. Separation masks for left/right
- 4. Estimated spectrograms for left/right



Score-Informed Audio Decompostion

Application: Separating left and right hands for piano

Ewert, Müller: Using Score-Informed Constraints for NMF-based Source Separation. Proc. ICASSP, 2012.

Chopin, Waltz Op. 64, No. 1



Original



Score-Informed Audio Decomposition

Application: Separating left and right hands for piano

Ewert, Müller: Using Score-Informed Constraints for NMF-based Source Separation. Proc. ICASSP, 2012.

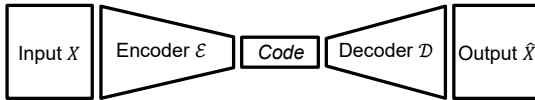
Chopin, Waltz Op. 64, No. 1



Conclusions (NMF)

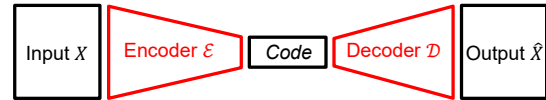
- NMF used for spectrogram decomposition
- Multiplicative update rules make it easy to constrain NMF model via zero initialization
- Exploiting score information to guide separation process (requires score-audio synchronization)
- Application: Separation of arbitrary note groups from given audio recording

Autoencoder



- Specific type of neural network
- Encoder: Compress input X into a low-dimensional code
- Decoder: Reconstruct output $\hat{X}$ from code

Autoencoder



- Specific type of neural network
- Encoder: Compress input X into a low-dimensional code
- Decoder: Reconstruct output $\hat{X}$ from code
- Goal: Learn parameters for encoder and decoder such that output is close to input with respect to some loss function:

$$\mathcal{L}(X, \hat{X}) \approx 0$$

NMF and Autoencoder (AE)

Smaragdis, Venkatesh: A Neural Network Alternative to Non-Negative Audio Models, Proc. ICASSP 2017.

NMF $V \approx W \cdot H = \hat{V}$

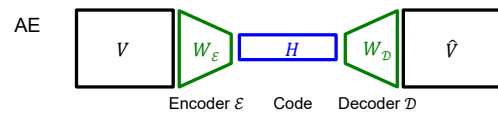
$V \approx WH$ implies $W^+V \approx H$ with pseudoinverse W^+

NMF and Autoencoder (AE)

Smaragdis, Venkatesh: A Neural Network Alternative to Non-Negative Audio Models, Proc. ICASSP 2017.

NMF $V \approx W \cdot H = \hat{V}$

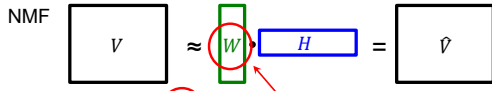
$V \approx WH$ implies $W^+V \approx H$ with pseudoinverse W^+



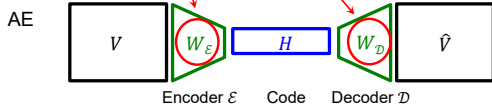
- Layer: $H = W_\epsilon V$
- Layer: $\hat{V} = W_\delta H$

NMF and Autoencoder (AE)

Smaragdis, Venkataramani: A Neural Network Alternative to Non-Negative Audio Models, Proc. ICASSP 2017.



$V \approx WH$ implies $W^+V \approx H$ with pseudoinverse W^+

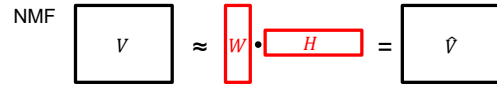


1. Layer: $H = W_\epsilon V$
2. Layer: $\hat{V} = W_d H$

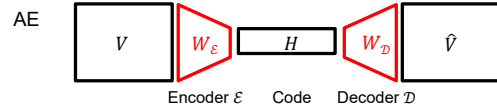
Fully connected network

NMF and Autoencoder (AE)

Smaragdis, Venkataramani: A Neural Network Alternative to Non-Negative Audio Models, Proc. ICASSP 2017.



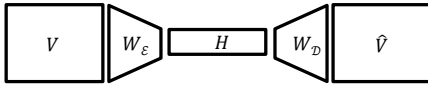
$V \approx WH$ implies $W^+V \approx H$ with pseudoinverse W^+



1. Layer: $H = W_\epsilon V$
2. Layer: $\hat{V} = W_d H$

NMF: Learn H and W
AE: Learn W_ϵ and W_d

Nonnegative Autoencoder (NAE)



1. Layer: $H = W_\epsilon V$
2. Layer: $\hat{V} = W_d H$

- How can one adjust the AE to simulate NMF?
- How can one achieve nonnegativity?
- How can one incorporate musical knowledge?
- ...

Nonnegative Autoencoder (NAE)

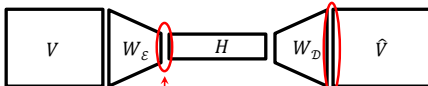


1. Layer: $H = W_\epsilon V$
2. Layer: $\hat{V} = W_d H$

$$\mathcal{L}(V, \hat{V}) = \|V - \hat{V}\|^2$$

- Loss function: same as in NMF

Nonnegative Autoencoder (NAE)

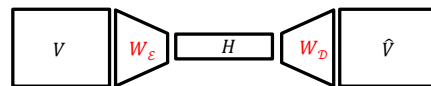


1. Layer: $H = \max(W_\epsilon V, 0)$
2. Layer: $\hat{V} = \max(W_d H, 0)$

$$\mathcal{L}(V, \hat{V}) = \|V - \hat{V}\|^2$$

- Loss function: same as in NMF
- Activation function (ReLU) makes H and $\hat{V}$ nonnegative

Nonnegative Autoencoder (NAE)



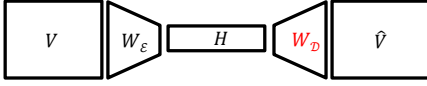
1. Layer: $H = \max(W_\epsilon V, 0)$
2. Layer: $\hat{V} = \max(W_d H, 0)$

$$\mathcal{L}(V, \hat{V}) = \|V - \hat{V}\|^2$$

$$W_d \leftarrow \max\left(W_d - \gamma \frac{\partial \mathcal{L}}{\partial W_d}, 0\right)$$

- Loss function: same as in NMF
- Activation function (ReLU) makes H and $\hat{V}$ nonnegative
- Projected gradient descent can be used to keep W_d (and W_ϵ) nonnegative

Musical Constraints

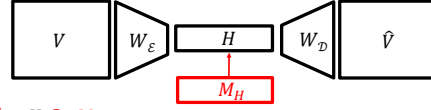


$$H = \max(W_\varepsilon V, 0)$$

$$\hat{V} = \max(W_D H, 0)$$

- Template constraints: Project certain entries in W_D to zero values (using projected gradient decent)

Musical Constraints



$$H' = H \odot M_H$$

$$\hat{V} = \max(W_D H', 0)$$

- Template constraints: Project certain entries in W_D to zero values (using projected gradient decent)
- Activation constraints: Use structured dropout by applying pointwise multiplication with binary mask M_H

Ewert, Sandler: Structured Dropout for Weak Label and Multi-Instance Learning and Its Application to Score-Informed Source Separation. Proc. ICASSP, 2017.

NAE with Multiplicative Update Rules

- Multiplicative update rules in NMF:
 - Preserve nonnegativity
 - Lead to fast convergence
- Question: Can one introduce multiplicative update rules to train network weights for NAE?

- Use in additive gradient descent $W^{(\ell+1)} = W^{(\ell)} - \gamma \cdot \frac{\partial \mathcal{L}}{\partial W}$
a suitable (adaptive) learning rate γ .

NAE with Multiplicative Update Rules

- Encoder:
 $H = W_\varepsilon V$
- Structured Dropout:
 $H' = H \odot M_H$
- Decoder:
 $\hat{V} = W_D H'$

Özer, Hansen, Zünner, Müller: Investigating Nonnegative Autoencoders for Efficient Audio Decomposition. Proc. EUSIPCO, 2022.

NAE with Multiplicative Update Rules

Özer, Hansen, Zünner, Müller: Investigating Nonnegative Autoencoders for Efficient Audio Decomposition. Proc. EUSIPCO, 2022.

- Encoder:
 $H = W_\varepsilon V$
- Structured Dropout:
 $H' = H \odot M_H$

$$W_{\varepsilon, rk}^{(\ell+1)} = W_{\varepsilon, rk}^{(\ell)} \cdot \frac{\left((W_D^\top V) \odot M_H \right) V^\top}{\left((W_D^\top W_D H' H'^\top) \odot M_H \right) V^\top}_{rk}$$

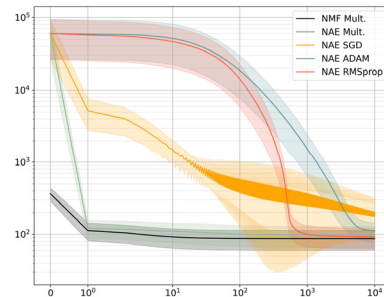
- Decoder:
 $\hat{V} = W_D H'$

$$W_{D, kr}^{(\ell+1)} = W_{D, kr}^{(\ell)} \cdot \frac{(V H'^\top)_{kr}}{(W_D^\top H' H'^\top)_{kr}}$$

Similar idea and computation as for NMF.

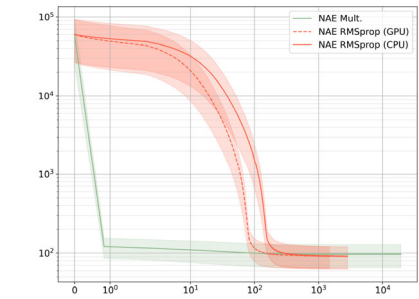
Approximation Loss

Özer, Hansen, Zünner, Müller: Investigating Nonnegative Autoencoders for Efficient Audio Decomposition. Proc. EUSIPCO, 2022.



Approximation Loss

Ozer, Hansen, Zünner, Müller: Investigating Nonnegative Autoencoders for Efficient Audio Decomposition. Proc. EUSIPCO, 2022.

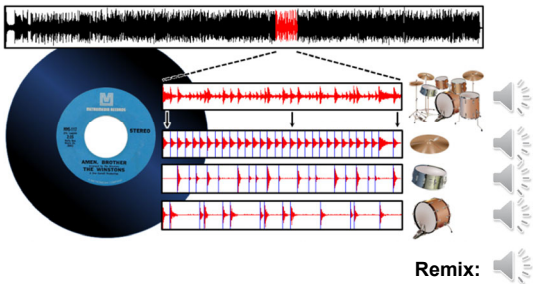


Conclusions (NAE)

- Simulation of NMF:
 - Decoder corresponds to NMF templates
 - Encoder learns a kind of pseudo-inverse
 - Code corresponds to NMF activations
- Nonnegativity can be achieved via
 - activation function (ReLU)
 - projected gradient descent
 - multiplicative update rules
- Musical knowledge can be integrated via
 - removing network weights (template constraints)
 - structured dropout (activation constraints)

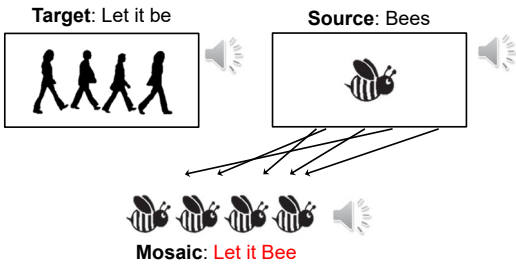
Informed Drum-Sound Decomposition

Dittmar, Müller: Reverse Engineering the Amen Break — Score-Informed Separation and Restoration Applied to Drum Recording. IEEE/ACM TASLP, 24(9): 1531–1543, 2016



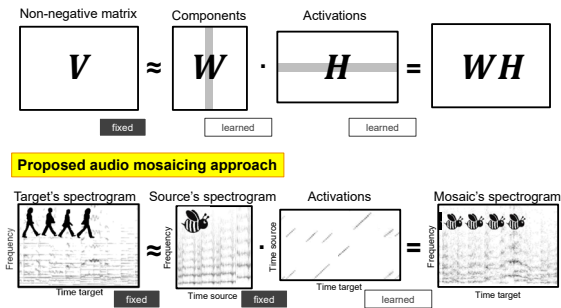
NMF-Inspired Audio Mosaicing

Driedger, Prätzsch, Müller: Let It Bee — Towards NMF-Inspired Audio Mosaicing. ISMIR, 350–356, 2015



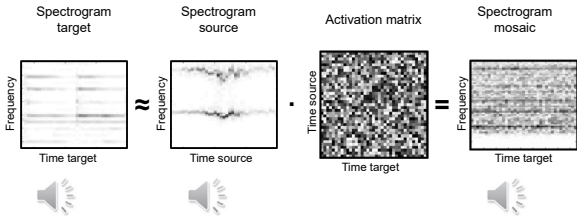
NMF-Inspired Audio Mosaicing

Driedger, Prätzsch, Müller: Let It Bee — Towards NMF-Inspired Audio Mosaicing. ISMIR, 350–356, 2015



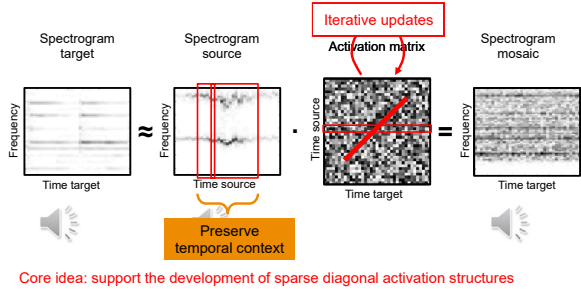
NMF-Inspired Audio Mosaicing

Driedger, Prätzsch, Müller: Let It Bee — Towards NMF-Inspired Audio Mosaicing. ISMIR, 350–356, 2015



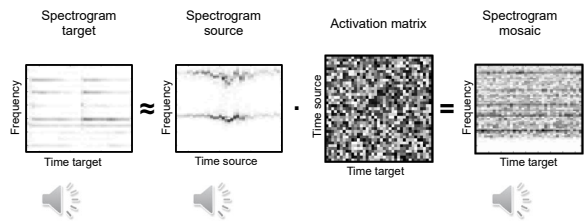
NMF-Inspired Audio Mosaicing

Driedger, Prätzlich, Müller: Let It Bee
— Towards NMF-Inspired Audio Mosaicing. ISMIR, 350–356, 2015



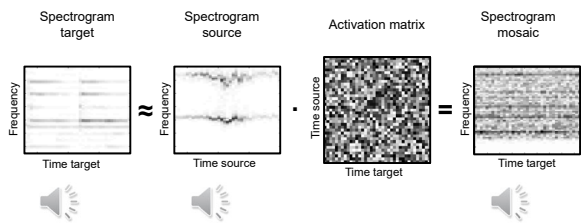
NMF-Inspired Audio Mosaicing

Driedger, Prätzlich, Müller: Let It Bee
— Towards NMF-Inspired Audio Mosaicing. ISMIR, 350–356, 2015



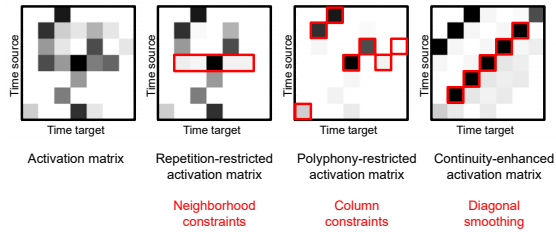
NMF-Inspired Audio Mosaicing

Driedger, Prätzlich, Müller: Let It Bee
— Towards NMF-Inspired Audio Mosaicing. ISMIR, 350–356, 2015



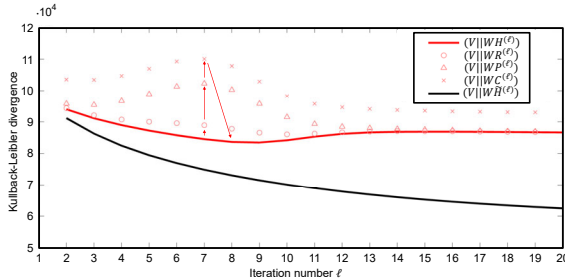
NMF-Inspired Audio Mosaicing

Driedger, Prätzlich, Müller: Let It Bee
— Towards NMF-Inspired Audio Mosaicing. ISMIR, 350–356, 2015



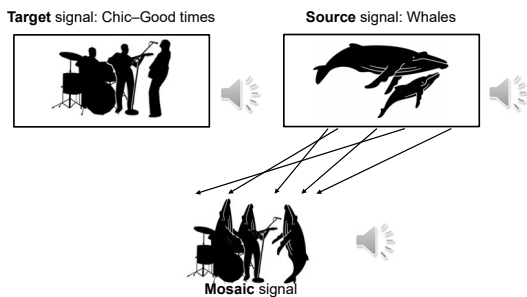
NMF-Inspired Audio Mosaicing

Driedger, Prätzlich, Müller: Let It Bee
— Towards NMF-Inspired Audio Mosaicing. ISMIR, 350–356, 2015



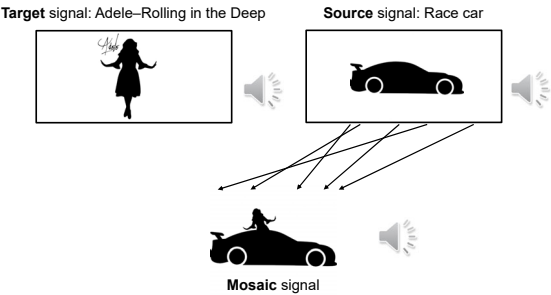
NMF-Inspired Audio Mosaicing

Driedger, Prätzlich, Müller: Let It Bee
— Towards NMF-Inspired Audio Mosaicing. ISMIR, 350–356, 2015



NMF-Inspired Audio Mosaicing

Driedger, Prätzlich, Müller: Let It Bee
— Towards NMF-Inspired Audio
Mosaicing. ISMIR, 350–356, 2015



Conclusions (Nonnegative Music Audio Decomposition)

- Spectrogram decomposition using NMF
- Integration of musical knowledge through constrained NMF
- Simulation of NMF using nonnegative autoencoders (NAEs)
- Related Topics:
 - Resynthesize of sound components
 - Differentiable Digital Signal Processing (DDSP)
 - Diffusion-based music synthesis
 - Generation of musical knowledge
 - Automatic music transcription
 - Dataset curation

References (NMF, NAE)

- Daniel Lee, Sebastian Seung: Algorithms for Non-Negative Matrix Factorization. Proc. NIPS, 2000.
- Sebastian Ewert, Meinard Müller: Using Score-Informed Constraints for NMF-Based Source Separation. Proc. ICASSP, 2012.
- Jonathan Driedger, Harald Grohganz, Thomas Prätzlich, Sebastian Ewert, Meinard Müller: Score-Informed Audio Decomposition and Applications. Proc. ACM-MM, 2013.
- Jonathan Driedger, Thomas Prätzlich, Meinard Müller: Let It Bee — Towards NMF-Inspired Audio Mosaicing. Proc. SMIR, 2015.
- Paris Smaragdis, Shrikant Venkataramani: A Neural Network Alternative to Non-Negative Audio Models. Proc. ICASSP, 2017.
- Sebastian Ewert, Mark B. Sandler: Structured Dropout for Weak Label and Multi-Instance Learning and Its Application to Score-Informed Source Separation. Proc. ICASSP, 2017.
- Meinard Müller: Fundamentals of Music Processing. Springer, 2021.
- Yigitcan Özer, Jonathan Hansen, Tim Zunner, Meinard Müller: Investigating Nonnegative Autoencoders for Efficient Audio Decomposition. Proc. EUSIPCO, 2022.